

Direct Method: $\bar{X} = \frac{\sum X}{N}$ Individual Series

Assumed Mean Method = $\bar{X} = A + \frac{\sum d}{N}$ Here $d = X - A$

Step deviation Method :

$$\bar{X} = A + \frac{\sum d'}{N} \times C$$

[midvalue = $\frac{L_1 + L_2}{2}$]

Discrete Series:

Direct Method: $\bar{X} = \frac{\sum Fx}{\sum F}$

Assumed Mean

$$\bar{X} = A + \frac{\sum fd}{\sum F}$$

Step Deviation Method:

$$\bar{X} = A + \frac{\sum fd'}{\sum F} \times C$$

Frequency Distribution

Direct: $\bar{X} = \frac{\sum fm}{\sum f}$

Assumed: $\bar{X} = A + \frac{\sum fd}{\sum F}$

Step deviation:

$$\bar{X} = A + \frac{\sum fd'}{\sum F} \times C$$

Here, C = Common factor
 $d' = \frac{d}{C}$

Calculated or correct mean

$$\bar{X} = \frac{\sum X(\text{wrong}) + (\text{correct value}) - (\text{incorrect value})}{N}$$

Calculation of Weighted Mean

$$\bar{X}_w = \frac{\sum wX}{\sum w}$$

Combined Mean

$$\bar{X}_{1,2} = \frac{\bar{X}_1 N_1 + \bar{X}_2 N_2}{N_1 + N_2}$$

Correlation:

Karl Pearson Coefficient of Correlation

Direct Method: $r = \frac{\sum xy}{\sqrt{\sum x^2} \sqrt{\sum y^2}}$ $x = X - \bar{X}$ $y = Y - \bar{Y}$

$$\bar{X} = \frac{\sum x}{N} \quad \bar{Y} = \frac{\sum y}{N}$$

Shortcut Method:

$$r = \frac{\sum d_x d_y - \frac{\sum d_x \times \sum d_y}{N}}{\sqrt{\sum d_x^2 - \frac{(\sum d_x)^2}{N}} \times \sqrt{\sum d_y^2 - \frac{(\sum d_y)^2}{N}}}$$

Here, $d_x = x - A$

$d_y = Y - A$ $A = \text{Assumed Mean}$

Step deviation Method:

$$r = \frac{\sum d_x' d_y' - \frac{\sum d_x' \times \sum d_y'}{N}}{\sqrt{\sum d_x'^2 - \frac{(\sum d_x')^2}{N}} \times \sqrt{\sum d_y'^2 - \frac{(\sum d_y')^2}{N}}}$$

$$\begin{aligned} d_x &= x - A \\ d_y &= Y - A \\ d_x' &= \frac{d_x}{c} \\ d_y' &= \frac{d_y}{c} \end{aligned}$$

Spearman Rank Correlation

(Rank not repeated)

$$D = R_1 - R_2 \quad r_s = 1 - \frac{6 \sum D^2}{N^3 - N}$$

(when rank is repeated)

$$r_s = 1 - \frac{6 \left[\sum D^2 + \frac{1}{12} (m_1^2 - m_1) + \frac{1}{12} (m_2^2 - m_2) - \dots \right]}{N^3 - N}$$

Median:

Individual Series

$$M = \frac{N+1}{2} \text{ th term}$$

Discrete Series

$$\text{Median} = \frac{N+1}{2} \text{ th term}$$

Continuous series

$$M = L_1 + \frac{\frac{N}{2} - f_0}{f} x_i$$

Mode:

In continuous series:

$$Z = L_1 + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} x_i$$

Calculation of Mode with Arithmetic Mean

$$Z = 3M - 2\bar{X}$$

Here, $Z = \text{Mode}$ $M = \text{Median}$ $\bar{X} = \text{Mean}$

Index Numbers

Simple Aggregative Method:

$$P_O_1 = \frac{\sum P_1}{\sum P_0} \times 100$$

Weighted Average of Price Relatives Method:

$$P_O_1 = \frac{\sum R W}{\sum W} \quad \text{Here } R = \frac{P_1}{P_0} \times 100$$

Weighted Aggregative Method:

(i) Laspeyres's Method : $P_O_1 = \frac{\sum P_1 q_0}{\sum P_0 q_0} \times 100$

(ii) Pasche's Method :

$$P_O_1 = \frac{\sum P_1 q_1}{\sum P_0 q_1} \times 100$$

(iii) Fisher's Method :

$$P_O_1 = \sqrt{\frac{\sum P_1 q_0}{\sum P_0 q_0}} \times \sqrt{\frac{\sum P_1 q_1}{\sum P_0 q_1}} \times 100$$

Consumer Price Index (CPI)

$$CPI = \frac{\sum P_1 q_0}{\sum P_0 q_0} \times 100 \quad (\text{Aggregative Expenditure Method})$$

Family Budget Method

$$CPI = \frac{\sum R W}{\sum W} \quad \text{Here, } W = P_0 q_0$$

$$R = \frac{P_1}{P_0} \times 100$$

↳ R = Current year's price relative of various items
 W = Weight of various items.

Simple Average of Price Relative Method

$$P_O_1 = \frac{\sum \left(\frac{P_1}{P_0} \times 100 \right)}{N}$$

N = no. of goods.